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Image Features

Readings:


Szeliski: Chapter 4.1

Some Slides adapted from Univ. of Washington

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Image matching/Correspondence problem



by [Diva Sian](#)

by [swashford](#)

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Harder case



by [Diva Sian](#)

by [scgbit](#)

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Even harder case



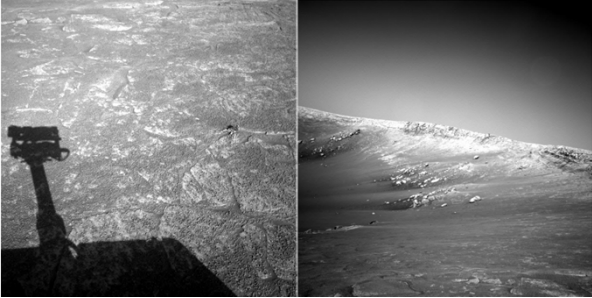
"How the Afghan Girl was Identified by Her Iris Patterns" Read the [story](#)



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Harder still?

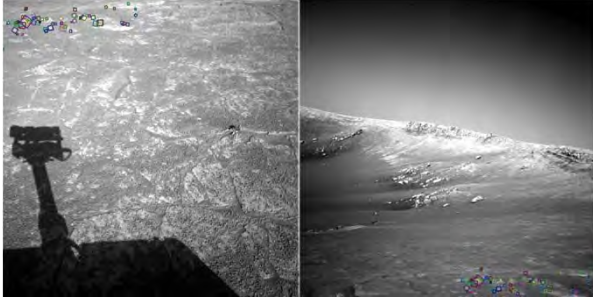


NASA Mars Rover images

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Answer below (look for tiny colored squares...)



NASA Mars Rover images with SIFT feature matches
Figure by Noah Snavely

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Image Matching

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Image Matching

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Invariant local features

Find features that are invariant to transformations

- geometric invariance: translation, rotation, scale
- photometric invariance: brightness, exposure, ...

Feature Descriptors

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Advantages of local features

Locality

- features are local, so robust to occlusion and clutter

Distinctiveness:

- can differentiate a large database of objects

Quantity

- hundreds or thousands in a single image

Efficiency

- real-time performance achievable

Generality

- exploit different types of features in different situations

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More motivation...

Feature points are used for:

- Image alignment (e.g., mosaics)
- 3D reconstruction
- Motion tracking
- Object recognition
- Indexing and database retrieval
- Robot navigation
- ... other

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What makes a good feature?

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Want uniqueness

Look for image regions that are unusual

- Lead to unambiguous matches in other images

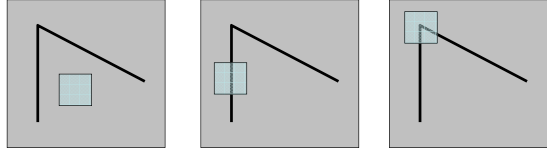
How to define “unusual”?

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Local measures of uniqueness

Suppose we only consider a small window of pixels

- What defines whether a feature is a good or bad candidate?



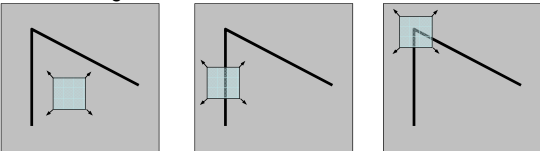
Slide adapted from Darya Frolova, Denis Simakov, Weizmann Institute.

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Feature detection

Local measure of feature uniqueness

- How does the window change when you shift it?
- Shifting the window in *any* direction causes a *big* change



“flat” region:
no change in all directions

“edge”:
no change along the edge direction

“corner”:
significant change in all directions

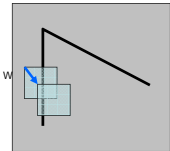
Slide adapted from Darya Frolova, Denis Simakov, Weizmann Institute.

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Feature detection: the math

Consider shifting the window W by (u,v)

- how do the pixels in W change?
- compare each pixel before and after by summing up the squared differences (SSD)
- this defines an SSD “error” of $E(u,v)$:



$$E(u, v) = \sum_{(x,y) \in W} [I(x + u, y + v) - I(x, y)]^2$$

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Small motion assumption

Taylor Series expansion of I :

$$I(x+u, y+v) = I(x, y) + \frac{\partial I}{\partial x}u + \frac{\partial I}{\partial y}v + \text{higher order terms}$$

If the motion (u,v) is small, then first order approx is good

$$I(x + u, y + v) \approx I(x, y) + \frac{\partial I}{\partial x}u + \frac{\partial I}{\partial y}v$$

$$\approx I(x, y) + [I_x \ I_y] \begin{bmatrix} u \\ v \end{bmatrix}$$

shorthand: $I_x = \frac{\partial I}{\partial x}$

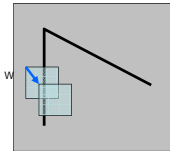
Plugging this into the formula on the previous slide...

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Feature detection: the math

Consider shifting the window W by (u,v)

- how do the pixels in W change?
- compare each pixel before and after by summing up the squared differences
- this defines an “error” of $E(u,v)$:



$$E(u, v) = \sum_{(x,y) \in W} [I(x + u, y + v) - I(x, y)]^2$$

$$\approx \sum_{(x,y) \in W} [I(x, y) + [I_x \ I_y] \begin{bmatrix} u \\ v \end{bmatrix} - I(x, y)]^2$$

$$\approx \sum_{(x,y) \in W} \left[[I_x \ I_y] \begin{bmatrix} u \\ v \end{bmatrix} \right]^2$$

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Feature detection: the math

This can be rewritten:

$$E(u, v) = \sum_{(x,y) \in W} [u \ v] \underbrace{\begin{bmatrix} I_x^2 & I_x I_y \\ I_y I_x & I_y^2 \end{bmatrix}}_H \begin{bmatrix} u \\ v \end{bmatrix}$$

For the example above

- You can move the center of the green window to anywhere on the blue unit circle
- Which directions will result in the largest and smallest E values?
- We can find these directions by looking at the eigenvectors of H

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Quick eigenvalue/eigenvector review

The **eigenvectors** of a matrix **A** are the vectors **x** that satisfy:

$$Ax = \lambda x$$

The scalar λ is the **eigenvalue** corresponding to **x**

- The eigenvalues are found by solving:

$$\det(A - \lambda I) = 0$$
- In our case, $A = H$ is a 2×2 matrix, so we have

$$\det \begin{bmatrix} h_{11} - \lambda & h_{12} \\ h_{21} & h_{22} - \lambda \end{bmatrix} = 0$$
- The solution: $\lambda_{\pm} = \frac{1}{2} \left[(h_{11} + h_{22}) \pm \sqrt{4h_{12}h_{21} + (h_{11} - h_{22})^2} \right]$

Once you know λ , you find **x** by solving

$$\begin{bmatrix} h_{11} - \lambda & h_{12} \\ h_{21} & h_{22} - \lambda \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = 0$$

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Feature detection: the math

This can be rewritten:

$$E(u, v) = \sum_{(x,y) \in W} [u \ v] \underbrace{\begin{bmatrix} I_x^2 & I_x I_y \\ I_y I_x & I_y^2 \end{bmatrix}}_H \begin{bmatrix} u \\ v \end{bmatrix}$$

Eigenvalues and eigenvectors of H

- Define shifts with the smallest and largest change (E value)
- x_+ = direction of largest increase in E.
- λ_+ = amount of increase in direction x_+ $Hx_+ = \lambda_+ x_+$
- x_- = direction of smallest increase in E. $Hx_- = \lambda_- x_-$
- λ_- = amount of increase in direction x_-

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Feature detection: the math

How are λ_+ , x_+ , λ_- , and x_- relevant for feature detection?

- What's our feature scoring function?

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Feature detection: the math

How are λ_+ , x_+ , λ_- , and x_- relevant for feature detection?

- What's our feature scoring function?

Want $E(u,v)$ to be *large* for small shifts in *all* directions

- the *minimum* of $E(u,v)$ should be large, over all unit vectors $[u \ v]$
- this minimum is given by the smaller eigenvalue (λ_-) of H

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Feature detection summary

Here's what you do

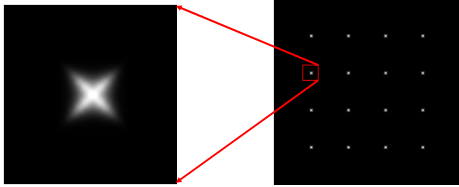
- Compute the gradient at each point in the image
- Create the H matrix from the entries in the gradient
- Compute the eigenvalues.
- Find points with large response ($\lambda_- >$ threshold)
- Choose those points where λ_- is a local maximum as features

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Feature detection summary

Here's what you do

- Compute the gradient at each point in the image
- Create the H matrix from the entries in the gradient
- Compute the eigenvalues.
- Find points with large response ($\lambda_1 > \text{threshold}$)
- Choose those points where λ_1 is a local maximum as features



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The Harris operator

λ_1 is a variant of the "Harris operator" for feature detection

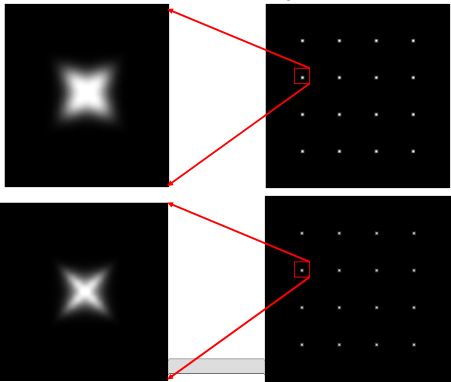
$$f = \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2}$$

$$= \frac{\text{determinant}(H)}{\text{trace}(H)}$$

- The *trace* is the sum of the diagonals, i.e., $\text{trace}(H) = h_{11} + h_{22}$
- Very similar to λ_1 , but less expensive (no square root)
- Called the "Harris Corner Detector" or "Harris Operator"
- Lots of other detectors, this is one of the most popular

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The Harris operator




Harris operator

λ_1

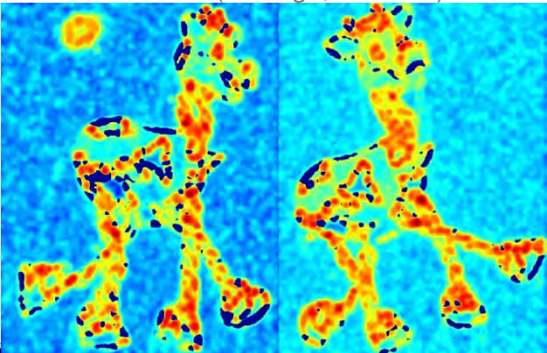
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Harris detector example




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f value (red high, blue low)

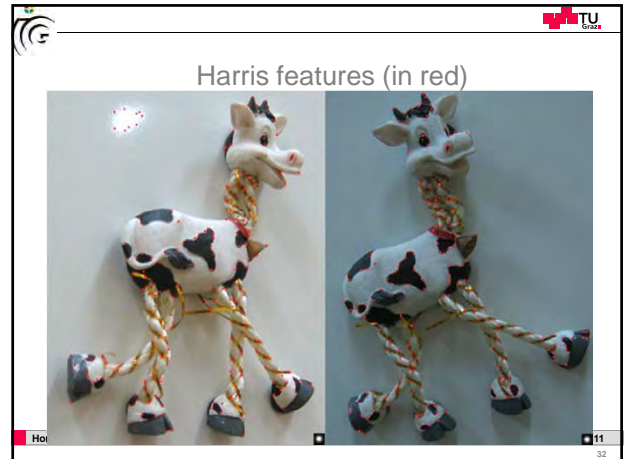
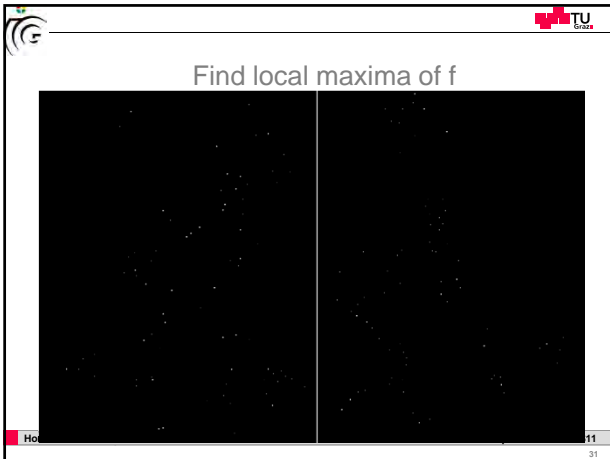


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Threshold ($f > \text{value}$)



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Invariance

Suppose you **rotate** the image by some angle
 – Will you still pick up the same features?

What if you change the brightness?

Scale?

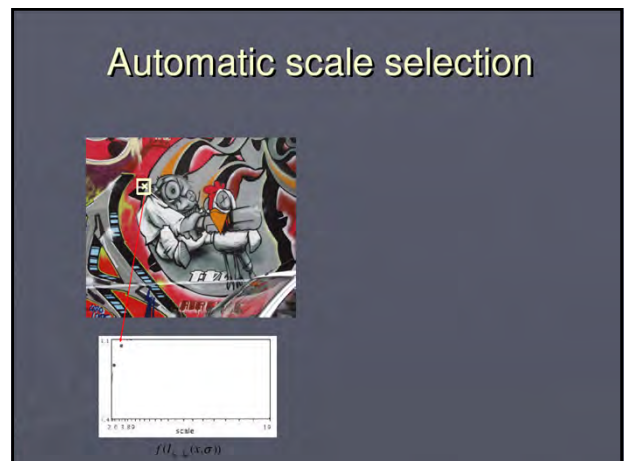
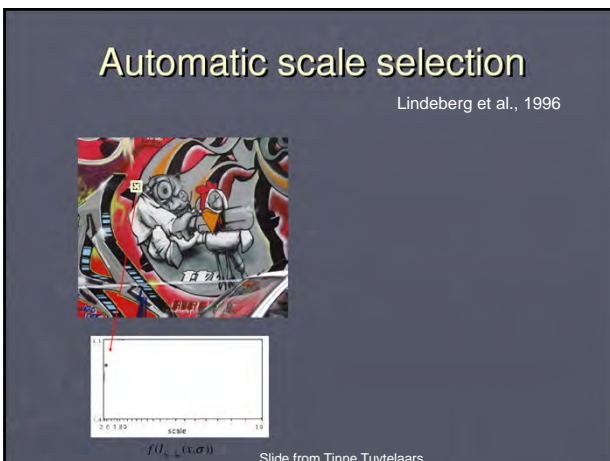
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Scale invariant detection

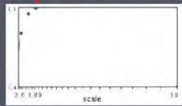
Suppose you're looking for corners

Key idea: find scale that gives local maximum of f
 – f is a local maximum in both position and scale
 – Common definition of f : Laplacian
 (or difference between two Gaussian filtered images with different sigmas)

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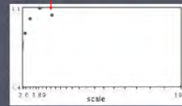


Automatic scale selection



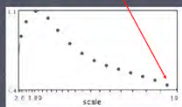
$$f(D_{x, \sigma}(x, \sigma))$$

Automatic scale selection



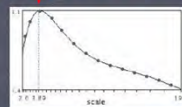
$$f(D_{x, \sigma}(x, \sigma))$$

Automatic scale selection



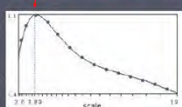
$$f(D_{x, \sigma}(x, \sigma))$$

Automatic scale selection

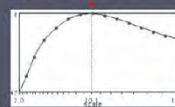


$$f(D_{x, \sigma}(x, \sigma))$$

Automatic scale selection



$$f(D_{x, \sigma}(x, \sigma))$$



$$f(D_{x, \sigma'}(x', \sigma'))$$

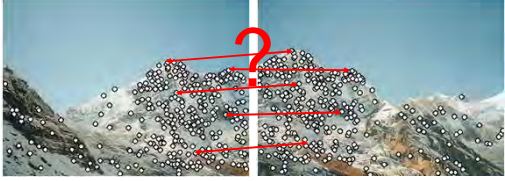
Automatic scale selection

Normalize: rescale to fixed size



Feature descriptors

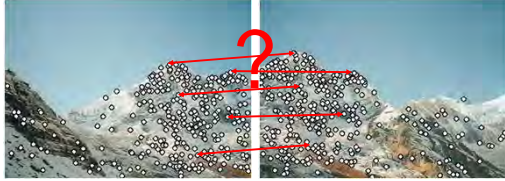
We know how to detect good points
Next question: **How to match them?**



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Feature descriptors

We know how to detect good points
Next question: **How to match them?**



Lots of possibilities (this is a popular research area)

- Simple option: match square windows around the point
- State of the art approach: SIFT
 - David Lowe, UBC <http://www.cs.ubc.ca/~lowe/keypoints/>

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Invariance

Suppose we are comparing two images I_1 and I_2

- I_2 may be a transformed version of I_1
- What kinds of transformations are we likely to encounter in practice?

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Invariance

Suppose we are comparing two images I_1 and I_2

- I_2 may be a transformed version of I_1
- What kinds of transformations are we likely to encounter in practice?

We'd like to find the same features regardless of the transformation

- This is called transformational **invariance**
- Most feature methods are designed to be invariant to
 - Translation, 2D rotation, scale
- They can usually also handle
 - Limited 3D rotations (SIFT works up to about 60 degrees)
 - Limited affine transformations (some are fully affine invariant)
 - Limited illumination/contrast changes

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How to achieve invariance

Need both of the following:


1. Make sure your detector is invariant
 - Harris is invariant to translation and rotation
 - Scale is trickier
 - common approach is to detect features at many scales using a Gaussian pyramid (e.g., MOPS)
 - More sophisticated methods find "the best scale" to represent each feature (e.g., SIFT)
2. Design an invariant feature *descriptor*
 - A descriptor captures the information in a region around the detected feature point
 - The simplest descriptor: a square window of pixels
 - What's this invariant to?
 - Let's look at some better approaches...

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Rotation invariance for feature descriptors

Find dominant orientation of the image patch

- This is given by \mathbf{x}_+ , the eigenvector of \mathbf{H} corresponding to λ_+
 - λ_+ is the *larger* eigenvalue
- Rotate the patch according to this angle



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Multiscale Oriented PatcheS descriptor

Take 40x40 square window around detected feature

- Scale to 1/5 size (using prefiltering)
- Rotate to horizontal
- Sample 8x8 square window centered at feature
- Intensity normalize the window by subtracting the mean, dividing by the standard deviation in the window

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Detections at multiple scales

Figure 1. Multi-scale Oriented Patches (MOPS) extracted at five pyramid levels from one of the Mater images. The boxes show the feature orientation and the region from which the descriptor vector is sampled.

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Scale Invariant Feature Transform

Basic idea:

- Take 16x16 square window around detected feature
- Compute edge orientation (angle of the gradient - 90°) for each pixel
- Throw out weak edges (threshold gradient magnitude)
- Create histogram of surviving edge orientations

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SIFT descriptor

Full version

- Divide the 16x16 window into a 4x4 grid of cells (2x2 case shown below)
- Compute an orientation histogram for each cell
- 16 cells * 8 orientations = 128 dimensional descriptor

Adapted from slide by David Lowe

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Properties of SIFT

Extraordinarily robust matching technique

- Can handle changes in viewpoint
 - Up to about 60 degree out of plane rotation
- Can handle significant changes in illumination
 - Sometimes even day vs. night (below)
- Fast and efficient—can run in real time
- Lots of code available
 - http://people.csail.mit.edu/albert/ladypack/wiki/index.php/known_implementations_of_SIFT

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Maximally Stable Extremal Regions

J.Matas et.al. "Distinguished Regions for Wide-baseline Stereo". BMVC 2002.

- Maximally Stable Extremal Regions
 - Threshold image intensities: $I > thresh$ for several increasing values of thresh
 - Extract connected components ("Extremal Regions")
 - Find a threshold when region is "Maximally Stable", i.e. local minimum of the relative growth
 - Approximate each region with an ellipse

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Feature matching

Given a feature in I_1 , how to find the best match in I_2 ?


1. Define distance function that compares two descriptors
2. Test all the features in I_2 , find the one with min distance

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Feature distance

How to define the difference between two features f_1, f_2 ?

- Simple approach is $SSD(f_1, f_2)$
 - sum of square differences between entries of the two descriptors
 - can give good scores to very ambiguous (bad) matches




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Feature distance

How to define the difference between two features f_1, f_2 ?

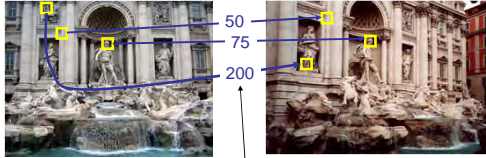
- Better approach: ratio distance = $SSD(f_1, f_2) / SSD(f_1, f_2')$
 - f_2 is best SSD match to f_1 in I_2
 - f_2' is 2nd best SSD match to f_1 in I_2
 - gives small values for ambiguous matches



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Evaluating the results

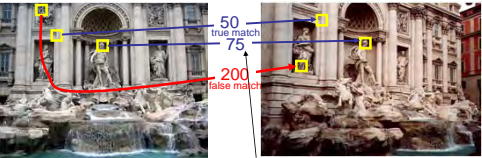
How can we measure the performance of a feature matcher?



feature distance

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True/false positives



feature distance

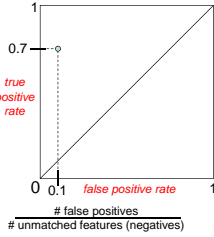
The distance threshold affects performance

- True positives = # of detected matches that are correct
 - Suppose we want to maximize these—how to choose threshold?
- False positives = # of detected matches that are incorrect
 - Suppose we want to minimize these—how to choose threshold?

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Evaluating the results

How can we measure the performance of a feature matcher?



true positives / # matching features (positives) true positive rate

false positives / # unmatched features (negatives) false positive rate

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Evaluating the results

How can we measure the performance of a feature matcher?

ROC curve ("Receiver Operator Characteristic")

$\frac{\# \text{ true positives}}{\# \text{ matching features (positives)}}$ true positive rate
 $\frac{\# \text{ false positives}}{\# \text{ unmatched features (negatives)}}$ false positive rate

ROC Curves

- Generated by counting # current/incorrect matches, for different thresholds
- Want to maximize area under the curve (AUC)
- Useful for comparing different feature matching methods
- For more info: http://en.wikipedia.org/wiki/Receiver_operating_characteristic

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More on feature detection/description

Affine Covariant Regions

Publications

Region detectors

- Harris-Affine & Hessian-Affine: K. Mikolajczyk and C. Schmid. Scale and Affine invariant interest point detectors. In ICV 1660-63-80, 2004. PDF
- MSER: J. Matas, O. Chum, M. Urban, and T. Pajdla. Robust wide baseline stereo from maximally stable extremal regions. In BMVC p. 384-393, 2002. PDF
- SIFT & SURF: T. Hornung and L. Van Gool. Matching widely separated views based on affine invariant regions. In ICV 1 (2) 61-85, 2004. PDF
- Subset regions: T. Kadir, A. Zisserman, and M. Brady. An affine invariant subset region detector. In ECCV p. 404-416, 2004. PDF

Region descriptors

- SIFT: D. Lowe. Distinctive image features from scale invariant keypoints. In ICCV 2(6) 91-110, 2004. PDF

Performance evaluation

- K. Mikolajczyk, T. Tomasi, C. Schmid, A. Zisserman, J. Matas, F. Schaffalitzky, T. Kadir and L. Van Gool. A comparison of affine region detectors. Technical Report, accepted to ICV PDF
- K. Mikolajczyk, C. Schmid. A performance evaluation of local descriptors. Technical Report, accepted to FAME PDF

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Lots of applications

Features are used for:

- Image alignment (e.g., mosaics)
- 3D reconstruction
- Motion tracking
- Object recognition
- Indexing and database retrieval
- Robot navigation
- ... other

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